

# **Private Adaptive Optimization with Side Information**

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#### Motivation \_\_\_\_\_ Adaptive optimizers (e.g., Adam, AdaGrad, RMSProp) are useful for a variety of ML tasks Performance may degrade significantly when trained with differential privacy (DP) Non-Private Private DP-SGD # epochs A baseline: directly plug in private gradients to estimate the statistics For example (vanilla DP-Adam) Estimates can be very noisy! 1. first privatize the gradients $\tilde{g}^{t} \leftarrow \frac{1}{|B|} \left( \sum_{i=1}^{n} \operatorname{clip}\left(g^{i,t}, C\right) + \mathcal{N}\left(0, \sigma^{2} C^{2}\right) \right)$ – Adam ----- DP-Adam 2. then plug in private gradients to any **10<sup>-5</sup>** adaptive optimization methods (e.g., Adam) **O** 10<sup>-</sup> $m^t \leftarrow \beta_1 m^t + (1 - \beta_1) \tilde{g}^t, \ v^t \leftarrow \beta_2 v^t + (1 - \beta_2) (\tilde{g}^t)^T$ Ö 10<sup>-9</sup> $w^{t+1} \leftarrow w^t - \alpha \frac{m^t}{\sqrt{v^t} + \epsilon}$

### Insights

#### Use side Information to approximate the preconditioner

Estimate gradient statistics on small public data at each iteration

- obtained via 'opt-out' users or proxy data
- can be in-distribution or out-of-distribution

Non-sensitive common knowledge about the training data

- easy to obtain before training  $\bigcirc$
- e.g., token frequencies in NLP  $\bigcirc$

Useful for both private and non-private training

### AdaDPS: Private Adaptive Optimization with Side Information

#### Option 1: With public data $x_{pub}$

2. update preconditioner  $A^t$  with recurrence  $\phi: A^t \leftarrow \phi(A^{t-1}, \hat{g}^t)$ 

#### **Option 2: Without public data**

 $A^{t}$  estimated via heuristics (e.g., TF-IDF values or feature frequencies)

(optional) maintain a momentum buffer using  $\hat{g}^t$ 

Privatize preconditioned gradients (in the simplest form)

$$\tilde{g}^t \leftarrow \frac{1}{|B|} \left( \sum_{i \in B} \operatorname{clip} \left( \frac{g^{i,t}}{A + \epsilon}, C \right) + . \right)$$

- preconditioning before privatizing the gradients (instead of the other order)
- can cover a range of adaptive methods

## **Convergence Analysis**

1. With public data, convex case, RMSProp updates

standard RMSPron rate

$$\sum_{j=1}^{d} \mathbb{E}\left[A_{j}^{T}\right] + \frac{\alpha}{\sqrt{T}} \prod_{t \in \mathcal{T}}^{T}$$

reduced DP noise when the gradients are sparse

2. Without public data, fixed preconditioner *A*, convex case, RMSProp updates

$$\frac{\alpha R + 1}{\sqrt{T}} \sum_{j=1}^{d} A_j + \frac{\alpha}{\sqrt{T}} \mathbb{E}\left[ \|\mathcal{N}\| \right]$$

One practical choice: feature frequencies for generalized linear models:  $A_i = \mathbb{E}[|x_i|] + \epsilon$ 

### Google Research





